

## Introduction

- Most current recommender systems are designed in the context of offline setting.
- It is desirable to provide real-time recommendations in large-scale scenarios.
- Some applications: social networks, movie/book suggestions, dating.

## Challenges

- Changing user preferences:
  - New items keep appearing.
  - The underlying user patterns keep changing.
  - This causes the recommendations to vary with time.
- In-core memory for memory-resident operations is quite limited.
- Classical methods like neighborhood-based and latent factor models have shortcomings.
  - They require a computationally expensive offline phase.
  - Factorizing large matrices is cumbersome when the said matrices are rapidly changing with time.

## The Setup

- The ratings are received in the format:  $\langle \text{userID}, \text{itemID}, \text{rating} \rangle$ .
- If rating is drawn from  $\{-1, +1\}$ , then let users who have given a rating of +1 to item  $i$  at time  $t$  be represented by  $P(i, t)$  and  $-1$  by  $N(i, t)$ .
- Since exact similarity computation is intensive, we compute it probabilistically by imposing a sort order on the users with the help of hash functions.
  - Use  $d$  mutually independent hash functions.
  - Each hash function takes in an identifier of a user and outputs a random number uniformly distributed in  $(0, 1)$ .

## Probabilistic Similarity

- Now, for a given sort order, what is the probability that the first user with a positive rating for item  $i$  is the same as the first user with a positive rating for item  $j$ ?
- This is the probability that both  $i$  and  $j$  take on the value +1 when at least one of them takes on the value of +1 given by:

$$\frac{P(i, t) \cap P(j, t)}{P(i, t) \cup P(j, t)}$$

- The above expression represents the similarity between items  $i$  and  $j$  with respect to positive ratings.

## Probabilistic Similarity

- The  $d$  mutually independent hash functions are applied to the user indices that have rated item  $j$  positively.
- For each hash function, the least hash value (*min-hash value*) among these positive users and the corresponding user index (*min-hash index*) are maintained.
- $d$  of such pairs are maintained for the  $n$  items seen which are easily updatable. This drastically reduces memory requirements.
- Similarly, the process is repeated for negatively rated items. The system can be extended for scenarios with multiple ratings as well.

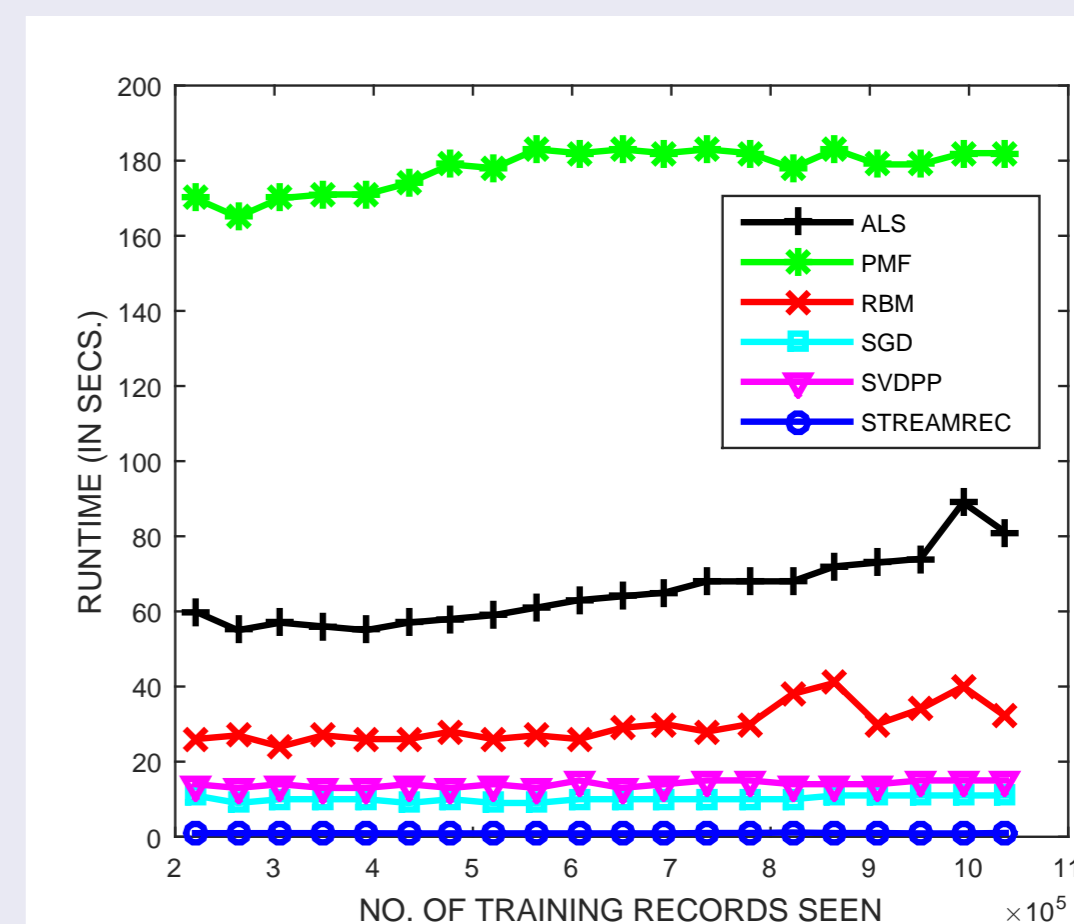
## Probabilistic Similarity

- How good is the quality of the similarity measure computed in this manner?
- Let  $R^+(i, j, t)$  be an approximation to the Jaccard coefficient computed by the min-hash approach and  $S^+(i, j, t)$  be the actual value. Then, we prove the following:
- Lower Tail Bound: For any  $\epsilon \in (0, 1)$ ,  $R^+(i, j, t)$  lies outside  $S^+(i, j, t)$  by a factor of  $(1 - \epsilon)$  with the probability:
 
$$P(R^+(i, j, t) < (1 - \epsilon) \cdot S^+(i, j, t)) \leq \exp(-d \cdot S^+(i, j, t) \cdot \epsilon^2/2)$$
- Upper Tail Bound: For any  $\epsilon \in (0, 2 \cdot e - 1)$ ,  $R^+(i, j, t)$  lies outside by a factor of  $(1 + \epsilon)$  with the probability:
 
$$P(R^+(i, j, t) > (1 + \epsilon) \cdot S^+(i, j, t)) \leq \exp(-d \cdot S^+(i, j, t) \cdot \epsilon^2/4)$$

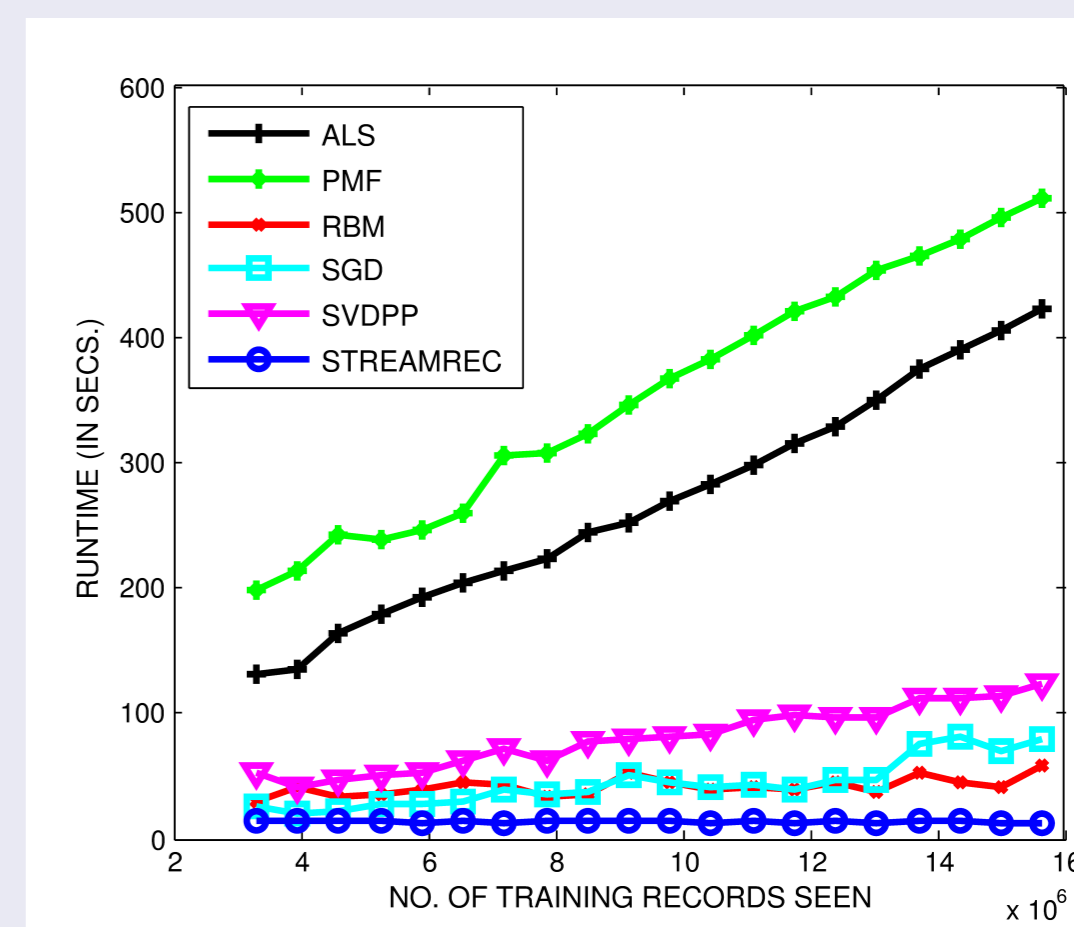
## Summary

- We address the problem of providing recommendations in a streaming setting.
- We provide an efficient algorithm to perform streaming recommendations using a probabilistic model.
- The proposed algorithm stores the rating matrix compactly and hence memory requirements are low.
- Our thorough experiments show that the proposed method performs as good or better than the state-of-the-art.

## Results



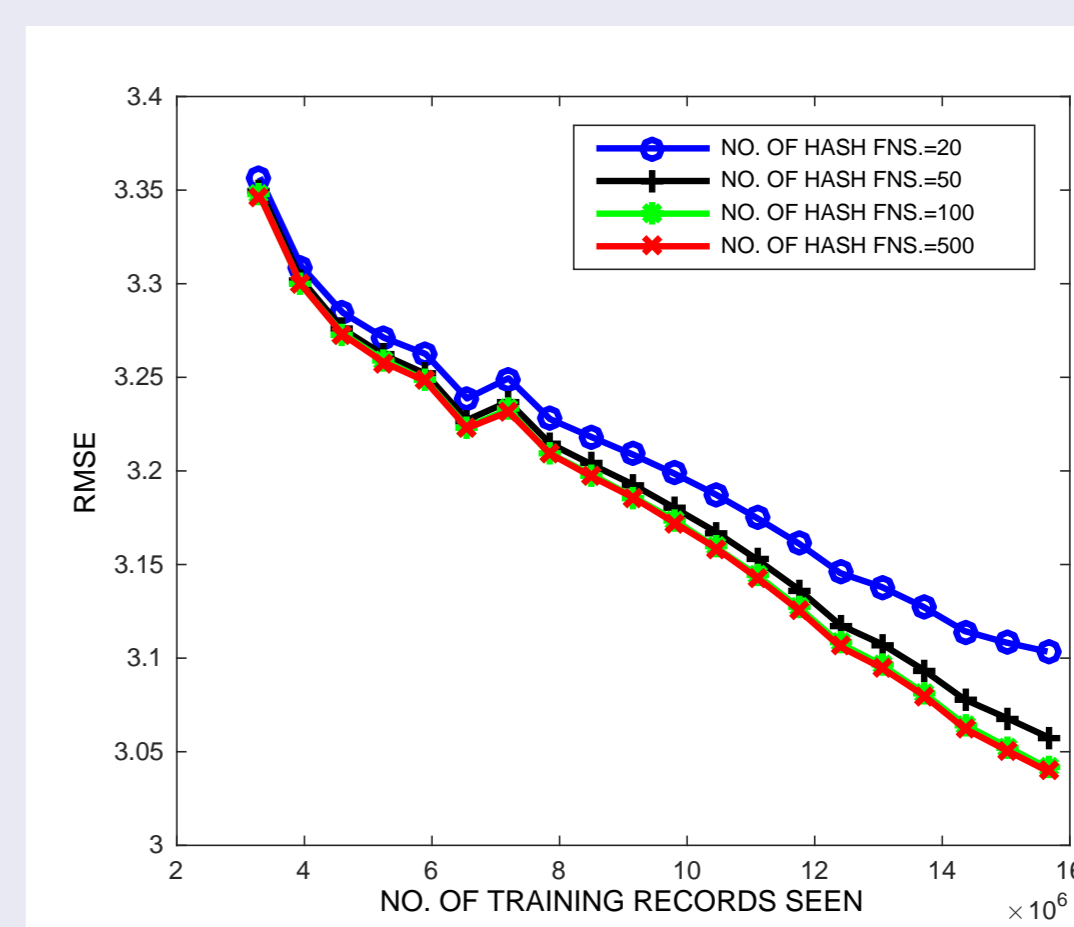
(a) Books Runtime



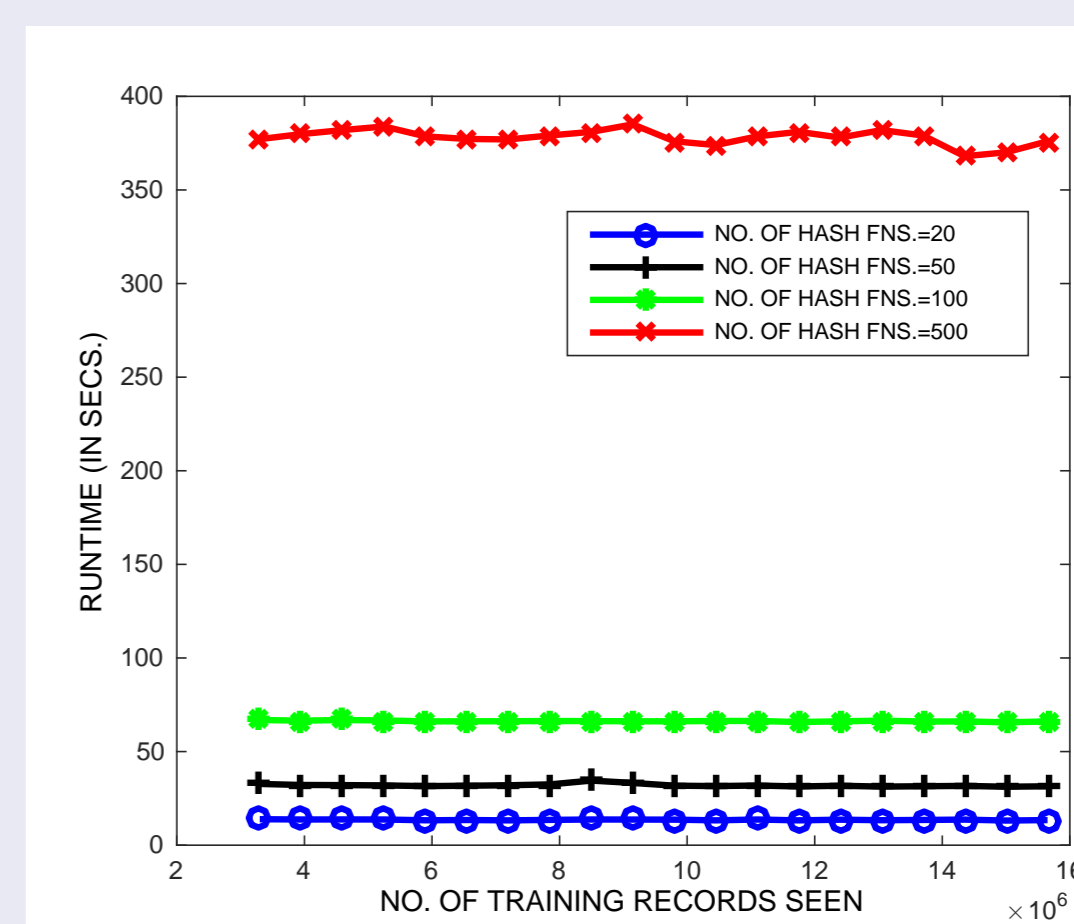
(b) Dating Runtime

Figure: Runtime

## Results



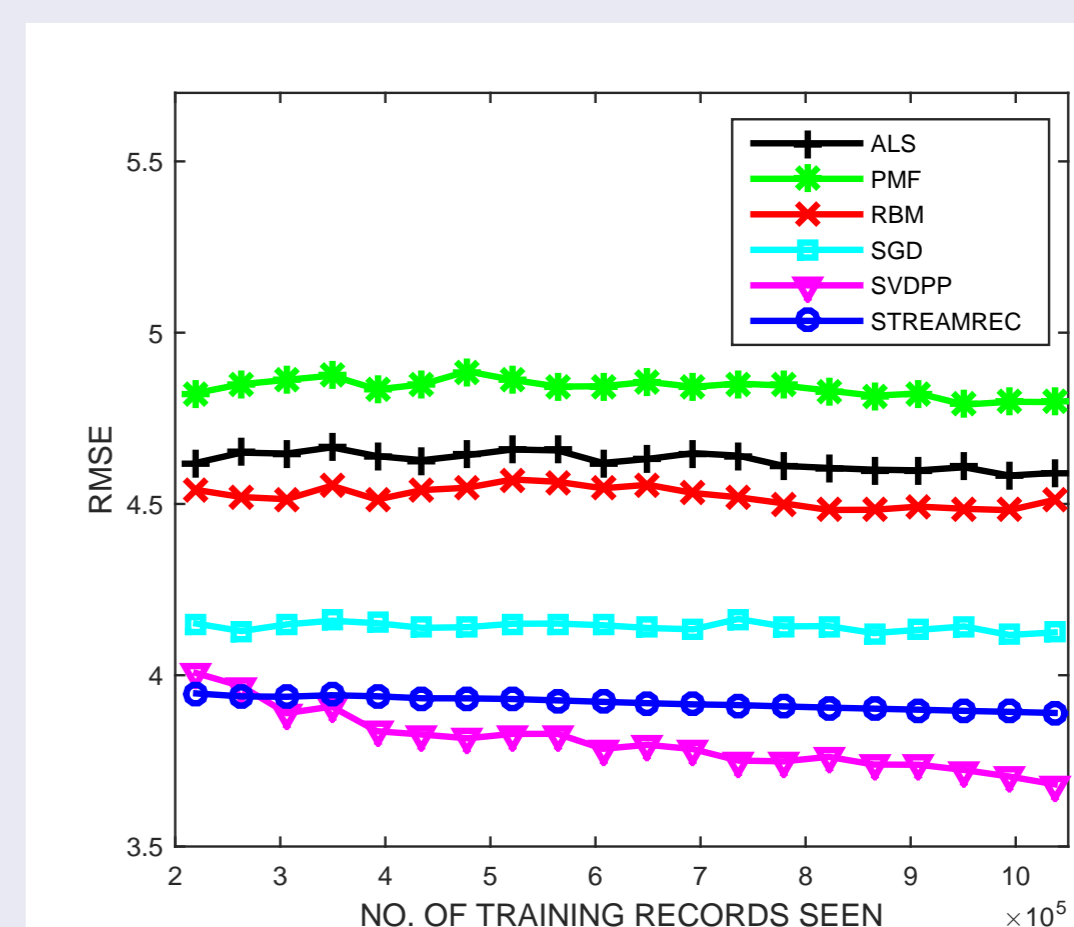
(a) Sensitivity Dating RMSE



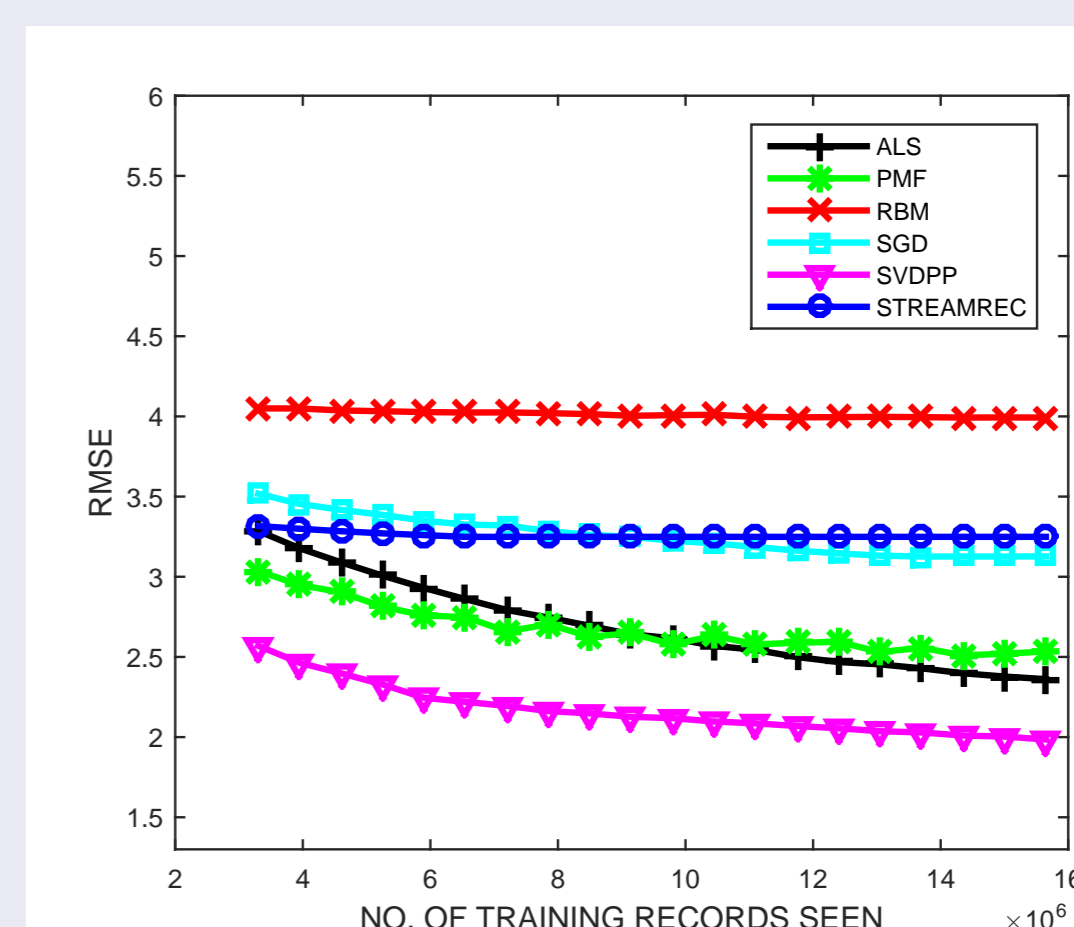
(b) Sensitivity Dating Runtime

Figure: Sensitivity

## Results



(a) Books RMSE



(b) Dating RMSE

Figure: Efficiency